| Course Title | Graph Theory and Applications in Networks |  |  |  |  |
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| Course Code | CSE414 |  |  |  |  |
| Course Type | Elective |  |  |  |  |
| Level | Bachelor (1st Cycle) |  |  |  |  |
| Year / Semester | $4^{\text {th }}$ Year / 8 ${ }^{\text {nd }}$ Semester |  |  |  |  |
| Teacher's Name | TBA |  |  |  |  |
| ECTS | 6 | Lectures / week | 3 hours / <br> 14 weeks | Laboratories / week | N/A |
| Course Purpose and Objectives | The course objective is to provide an introduction to the theory of graphs. The course starts from basic definitions and examples and moves to cover a broad range of topics. Applications of Graph Theory in Computer Science will be discussed throughout. Emphasis will be given to reading, understanding and developing graph theoretical proofs. Topics include: degrees, paths, trees, cycles, Eulerian circuits, bipartite graphs, extremality, matchings, connectivity, network flows, vertex and edge colorings, Hamiltonian cycles and planarity. |  |  |  |  |
| Learning Outcomes | Upon successful completion of the course, students will be able to: <br> - Model problems in computer science using graphs and trees. <br> - Describe precise and accurate mathematical definitions of objects in graph theory; <br> - Validate and critically assess a mathematical, graphtheoretical proof; <br> - Formulate mathematical, graph-theoretical proofs based on definitions; <br> - Write about graph theory in a coherent and technically accurate manner. |  |  |  |  |
| Prerequisites | CSE400 |  | quisites | None |  |
| Course Content | Introduction: What is graph theory useful for? Examples of graphsdirected, undirected, acyclic, complete, bipartite. Incidence and adjacency. Example application: shortest path problem. Example application: three houses problem. Example application: matching jobs to applicants. Directed graphs ,Orientations of an undirected graph, Tournaments, Euler tours in digraphs, Application: rotational position sensor, Into to graphical models. |  |  |  |  |


|  | Trees, Application: planning an efficient road network. Definition of trees. Properties of trees: number of edges and vertices, degree of vertices, cut edges. Spanning trees. Kruskal's algorithm. <br> Connectivity, Cayley's formula, Cut vertices, vertex cuts, edge cuts. Blocks; the block detection algorithm challenge. Connectivity and edge-connectivity. Application: designing resilient computer networks. <br> Euler tours and Chinese postmen The seven bridges of Königsberg Conditions for Eulerian graphs. The Chinese postman problem, Fleury's algorithm, Hamilton paths. <br> Matchings and coverings, Matches, perfect matches, matches in bipartite graphs, Personnel assigment problem, Hall's theorem. The marriage theorem. The Gale-Shapley algorithm. <br> Connectivity and Paths, Cuts and Connectivity, k-connected Graphs, Network Flow Problems <br> Graph Coloring, Vertex Colorings, Upper Bounds, Brooks' Theorem, k-chromatic Graphs, Perfect Graphs. <br> Edges and Cycles, Line Graphs and Edge-coloring, Proper colourings, edge chromaticity. Hamiltonian Cycles <br> Planar Graphs, Embeddings and Euler's Formula, Drawings in the Plane, Dual Graphs, Characterization of Planar Graphs, Parameters of Planarity |
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| Teaching Methodology | Face- to- face |
| Bibliography | Douglas B West, Introduction To Graph Theory, 2nd edition, Prentice Hall. <br> Geir Agnarsson, Graph Theory: Modeling, Applications, and Algorithms, Pearson. <br> Raymond Greenlaw,Robin J. Wilson, Introduction to Graph Theory, Pearson. <br> Reinhard Diestel, Graph Theory. Springer-Verlag. |


|  | Graph Theory with Applications to Engineering and Computer <br> Science, Dover publications. |
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| Assessment | Mid - Term Examination <br> Final Examination <br> Assignments/Lab <br> Class Participation and attendance |
| Language | English |

